

Primjer 6.1

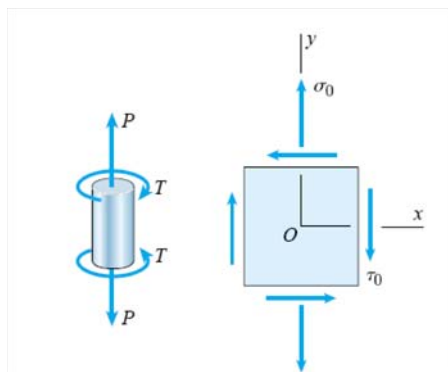
Vratilo elise helikoptera pokreće elisu koja obezbjeđuje podižuću silu kako bi se helikopter održao u zraku. Kao posljedica se javlja kombinacija uvijanja i aksijalnog naprežanja. Ako je prečnik vratila 50 mm, moment uvijanja 2.4 kNm i zatežuća sila 125 kN, odrediti maksimalan zatežući, maksimalan pritisni napon ,te maksimalan tangencijalni napon vratila.



$$d := 50\text{mm} \quad \underline{A} := \frac{d^2 \cdot \pi}{4} \quad I_0 := \frac{d^3 \cdot \pi}{16} \quad r := \frac{d}{2}$$

$$\underline{T} := 2.4\text{kN}\cdot\text{m}$$

$$\underline{F} := 125\text{kN}$$



$$\sigma_z := \frac{F}{A} = 63.662 \text{ MPa}$$

$$\tau := \frac{T}{I_0} = 97.785 \text{ MPa}$$

$$\sigma_{12} = \frac{\sigma_x + \sigma_y}{2} + pm \cdot \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau^2} \quad \sigma_x = 0 \quad \sigma_y = \sigma_z$$

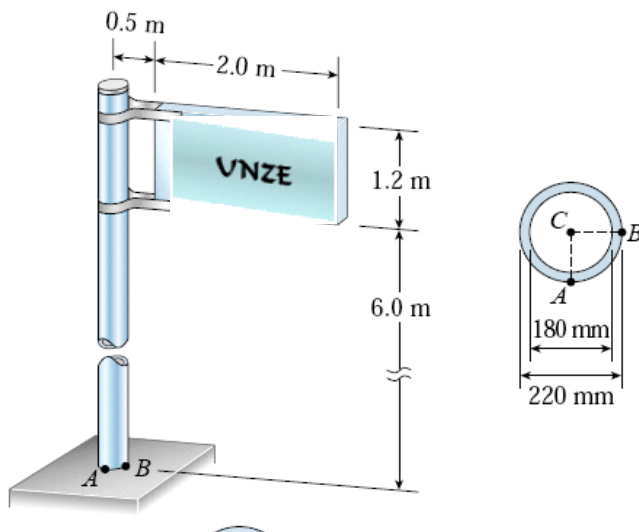
$$\sigma_1 := \frac{\sigma_z}{2} + \sqrt{\left(\frac{0 - \sigma_z}{2}\right)^2 + \tau^2} = 134.666 \text{ MPa}$$

$$\sigma_2 := \frac{\sigma_z}{2} - \sqrt{\left(\frac{0 - \sigma_z}{2}\right)^2 + \tau^2} = -71.004 \text{ MPa}$$

$$\tau_{\max} := \sqrt{\left(\frac{0 - \sigma_z}{2}\right)^2 + \tau^2} = 102.835 \text{ MPa}$$

Primjer 6.2

Tabla dimenzija 2 x 1.2 m, kao na slici, postavljena je na stub u obliku cijevi unutrašnjeg prečnika 220 mm i vanjskog prečnika 180 mm. Početak znaka je 0.5 m od ose cijevi stuba, te 6 m iznad zemlje. Odrediti glavne napone i maksimalan tangencijalni napon u tačkama A i B na dnu stuba ako na znak djeluje vjetar koji izaziva pritisak 2 kPa.



$$d_s := 220\text{mm} \quad d_u := 180\text{mm}$$

$$h := 1.2\text{m} \quad w := 2\text{m} \quad \underline{A} := h \cdot w$$

$$\underline{e} := 0.5\text{m}$$

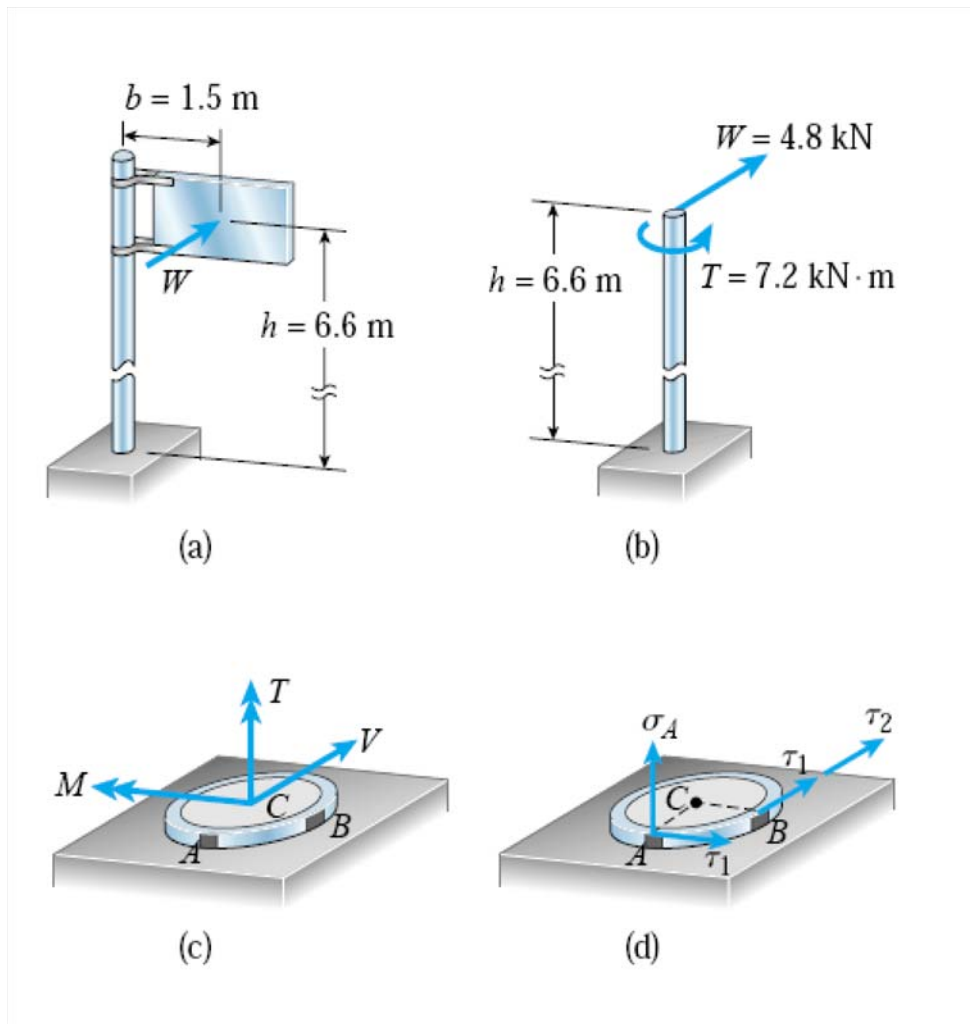
$$\underline{l} := 6\text{m}$$

$$p := 2\text{kPa}$$

$$I := \frac{d_s^4 - d_u^4}{64} \cdot \pi$$

$$I_0 := 2I$$

$$A_p := \frac{d_s^2 - d_u^2}{4} \cdot \pi$$



Moment uvijanja i tangencijalna sila

$$T := p \cdot A \cdot \left(e + \frac{w}{2} \right) = 7.2 \text{ kN} \cdot \text{m}$$

$$V := p \cdot A = 4.8 \text{ kN}$$

Moment savijanja

$$M := p \cdot A \cdot \left(1 + \frac{h}{2} \right) = 31.68 \text{ kN} \cdot \text{m}$$

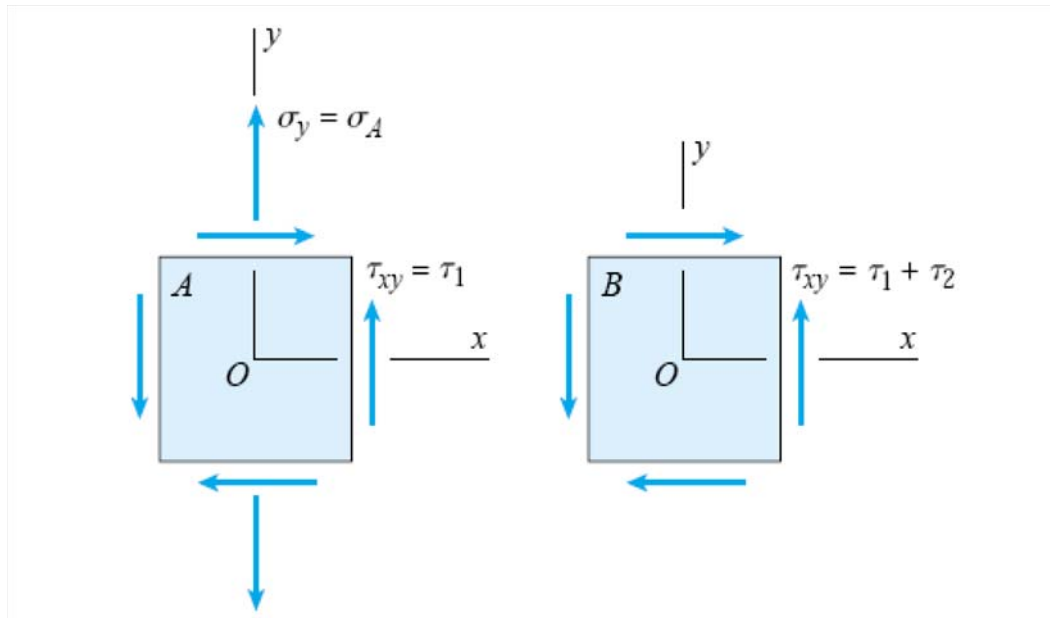
Naponi u tačkama A i B

$$\sigma_A := \frac{M \cdot \frac{d_s}{2}}{I} = 54.913 \text{ MPa}$$

$$\tau_T := T \cdot \frac{\frac{d_s}{2}}{I_0} = 6.24 \text{ MPa}$$

$$\tau_V := \frac{4V}{3A_p} \cdot \left[\frac{\left(\frac{d_s}{2} \right)^2 + \frac{d_s}{2} \cdot \frac{d_u}{2} + \left(\frac{d_u}{2} \right)^2}{\left(\frac{d_s}{2} \right)^2 + \left(\frac{d_u}{2} \right)^2} \right] = 0.759 \text{ MPa}$$

Elementi napona



$$\sigma_{12} = \frac{\sigma_x + \sigma_y}{2} \pm \text{pm} \cdot \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau^2}$$

Tačka A

$$\sigma_x = 0 \quad \sigma_y = \sigma_A \quad \tau := \tau_T$$

$$\sigma_{1A} := \frac{\sigma_A}{2} + \sqrt{\left(\frac{0 - \sigma_A}{2}\right)^2 + \tau_T^2} = 55.613 \text{ MPa}$$

$$\sigma_{2A} := \frac{\sigma_A}{2} - \sqrt{\left(\frac{0 - \sigma_A}{2}\right)^2 + \tau_T^2} = -0.7 \text{ MPa}$$

$$\tau_{\max A} := \sqrt{\left(\frac{0 - \sigma_A}{2}\right)^2 + \tau_T^2} = 28.157 \text{ MPa}$$

Tačka B

$$\sigma_x = \sigma_y = 0$$

$$\tau := \tau_T + \tau_V$$

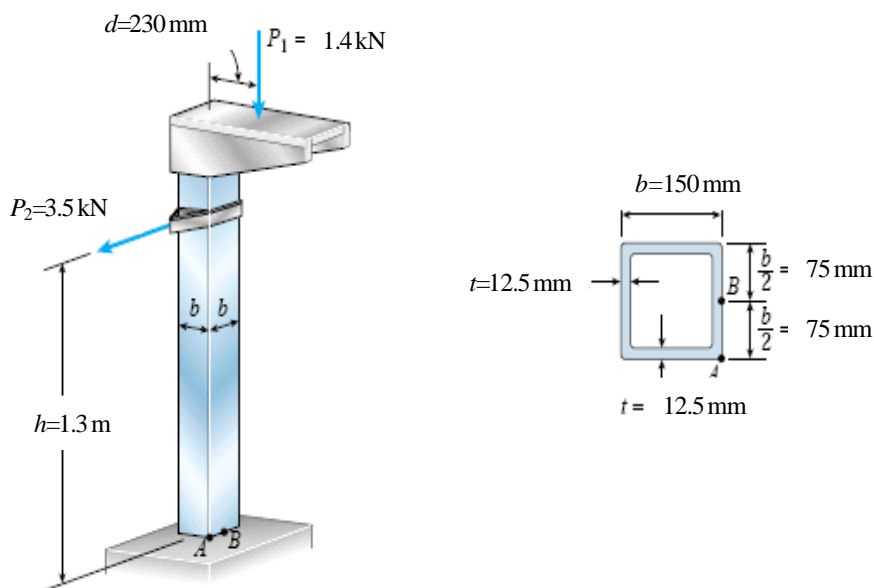
$$\sigma_{1\Lambda} := \tau = 6.999 \text{ MPa}$$

$$\sigma_{2\Lambda} := -\tau = -6.999 \text{ MPa}$$

$$\tau_{\max\Lambda} := \tau = 6.999 \text{ MPa}$$

Primjer 6.3

Stub od cijevi kvadratnog poprečnog presjeka služi kao nosač horizontalne platforme. Vanjska dimezija cijevi je 15 cm a debljina stjenke je 12.5 mm. Platforma ima dimen 170 x 610 mm i nosi kontinuirano opterećenje od 140 kPa koje djeluje na gornjoj površini. Rezultanta ovog opterećenja je vertikalna sila od 14.5 kN i djeluje na sredini platforme, udaljenom 230 mm od ose cijevi. Druga sila od 3.5 kN djeluje horizontalno na stub 1.3 m od osnove. Odrediti glavne normalne napone i maksimalan tangencijalni napon u tačkama A i B na osnovi.



$$d := 230 \text{ mm} \quad h := 1.3 \text{ m}$$

$$b := 150 \text{ mm} \quad t := 12.5 \text{ mm} \quad A_p := b^2 - (b - 2t)^2$$

$$I := \frac{b^4 - (b - 2t)^4}{12}$$

$$A_m := 2t \cdot (b - 2t)$$

$$P_1 := 14.5 \text{ kN}$$

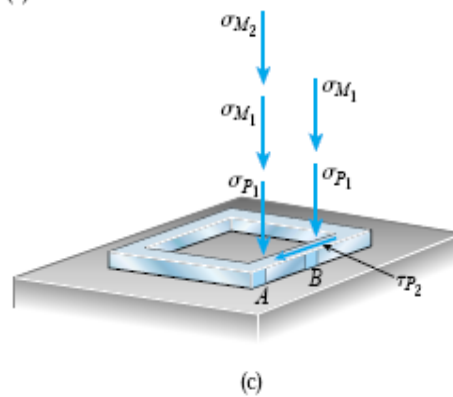
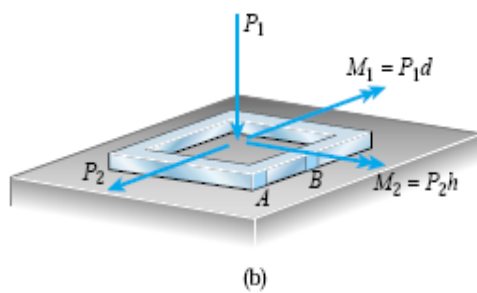
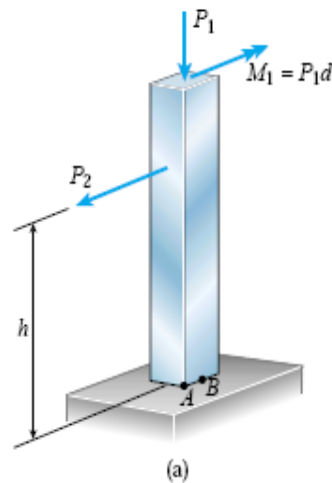
$$P_2 := 3.5 \text{ kN}$$

Naponi u tačkama A i B

$$M_1 := P_1 \cdot d = 3.335 \times 10^3 \text{ N}\cdot\text{m}$$

$$M_2 := P_2 \cdot h = 4.55 \times 10^3 \text{ N}\cdot\text{m}$$

$$\sigma_{P1} := \frac{P_1}{A_p} = 2.109 \text{ MPa}$$



$$\sigma_{12} = \frac{\sigma_x + \sigma_y}{2} + pm \cdot \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau^2}$$

$$\sigma_{M1} := \frac{M_1 \cdot \frac{b}{2}}{I} = 11.451 \text{ MPa}$$

$$\tau_{P2} := \frac{P_2}{A_m} = 1.12 \text{ MPa}$$

$$\sigma_{M2} := \frac{M_2 \cdot \frac{b}{2}}{I} = 15.623 \text{ MPa}$$

Tačka A - jednoosno aksijalno naprezanje

$$\sigma_A := -(\sigma_{P1} + \sigma_{M1} + \sigma_{M2}) = -29.184 \text{ MPa} \quad \text{pritisak!!!}$$

$$\tau_{\max A} := \left| \frac{\sigma_A}{2} \right| = 14.592 \text{ MPa}$$

Tačka B

$$\sigma_x = 0 \quad \sigma_y = \sigma_A \quad \tau_{xy} = \tau_{P2}$$

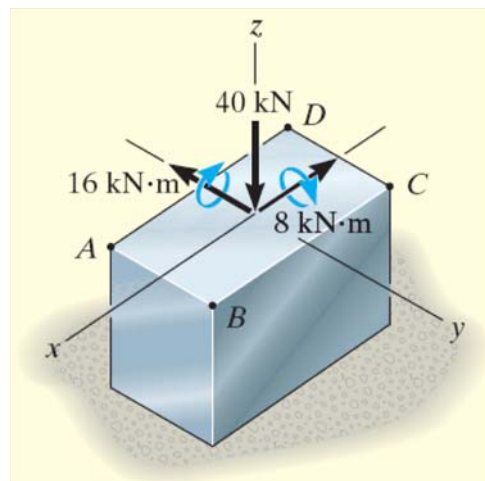
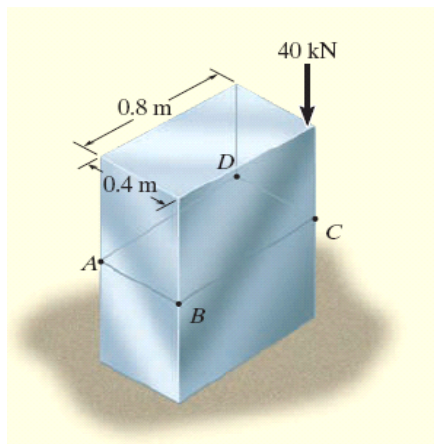
$$\sigma_{1A} := \frac{\sigma_A}{2} + \sqrt{\left(\frac{0 - \sigma_A}{2}\right)^2 + \tau_{P2}^2} = 0.043 \text{ MPa}$$

$$\sigma_{2A} := \frac{\sigma_A}{2} - \sqrt{\left(\frac{0 - \sigma_A}{2}\right)^2 + \tau_{P2}^2} = -29.227 \text{ MPa}$$

$$\tau_{\max A} := \sqrt{\left(\frac{0 - \sigma_A}{2}\right)^2 + \tau_{P2}^2} = 14.635 \text{ MPa}$$

Primjer 6.4

Pravougaoni blok izložen je vertikalnoj sili od 40 kN, s napadnom tačkom u uglu bloka (slika). Odrediti najveći napon koji djeluje u presjeku $ABCD$. Težinu bloka zanemarit



$$b := 0.4\text{ m} \quad w := 0.8\text{ m} \quad I_x := \frac{w \cdot b^3}{12} \quad I_y := \frac{b \cdot w^3}{12} \quad \underline{\underline{A}} := b \cdot w$$

$$\underline{\underline{F}} := 40\text{ kN}$$

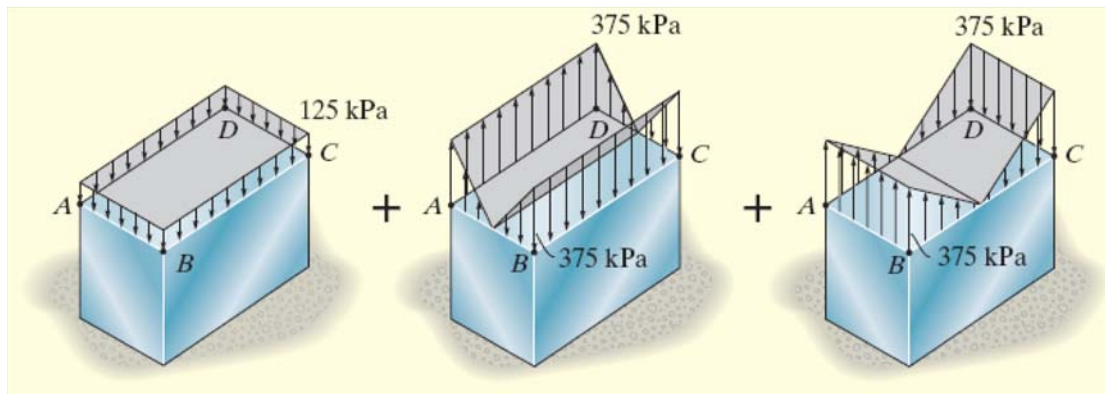
$$M_x := F \cdot \frac{b}{2} = 8 \times 10^3 \text{ N}\cdot\text{m} \quad M_y := F \cdot \frac{w}{2} = 1.6 \times 10^4 \text{ N}\cdot\text{m}$$

Komponente napona

$$\sigma := \frac{F}{A} = 0.125 \text{ MPa}$$

$$\sigma_{\text{max1}} := \frac{M_x \cdot \frac{b}{2}}{I_x} = 3.75 \times 10^5 \text{ Pa}$$

$$\sigma_{\text{max2}} := \frac{M_y \cdot \frac{w}{2}}{I_y} = 3.75 \times 10^5 \text{ Pa}$$



$$\sigma_C := -\sigma - \sigma_{\max 1} - \sigma_{\max 2} = -0.875 \text{ MPa}$$